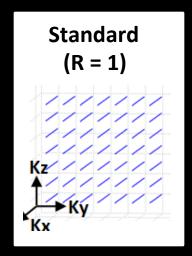


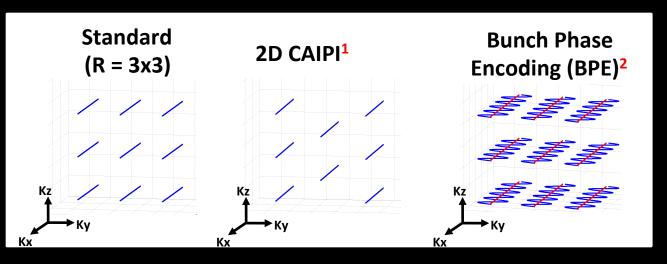
Wave-CAIPI: Highly Accelerated 3D Imaging with Reduced g-factor Penalty

B. Bilgic^{1,2}, B. A. Gagoski^{2,3}, S.F. Cauley^{1,2}, A.P. Fan^{1,4}, J.R. Polimeni^{1,2}, P.E. Grant^{2,3}, L.L.Wald^{1,2,5}, K. Setsompop^{1,2}

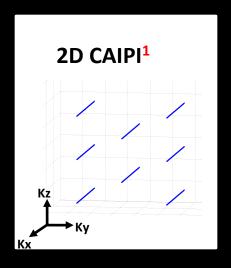
- 1 Martinos Center for Biomedical Imaging, Charlestown, MA,
- 2 Harvard Medical School, Boston, MA
- 3 Boston Children's Hospital, Boston, MA
- 4 Department of Electrical Engineering and Computer Science, MIT, Cambridge, MA
- 5 Harvard-MIT Division of Health Sciences and Technology, MIT, Cambridge, MA

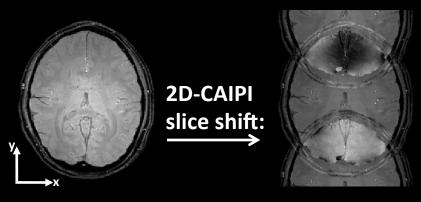
Recent modifications to rectilinear k-space sampling have provided more robust reconstructions of highly under-sampled datasets.



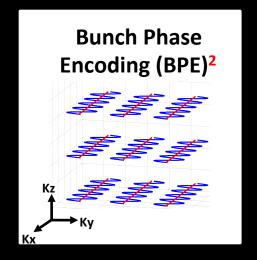


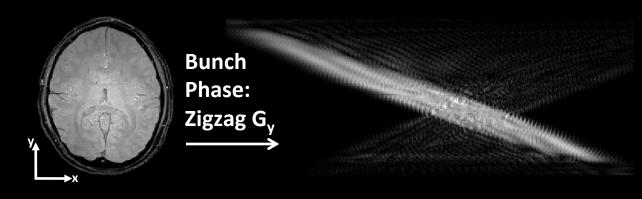
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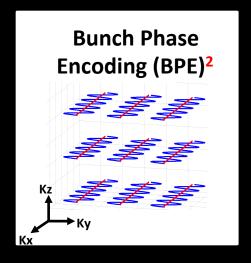


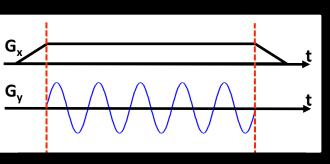
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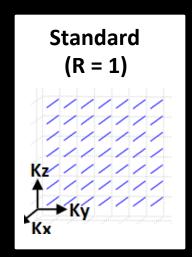


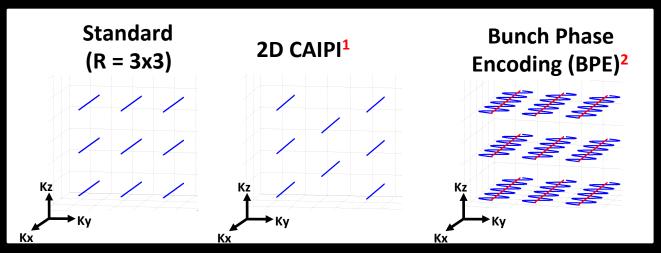




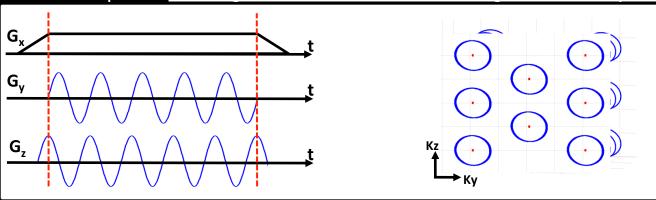
Bunch
Phase:
Zigzag G_y

 Recent modifications to rectilinear k-space sampling have provided more robust reconstructions of highly under-sampled datasets.



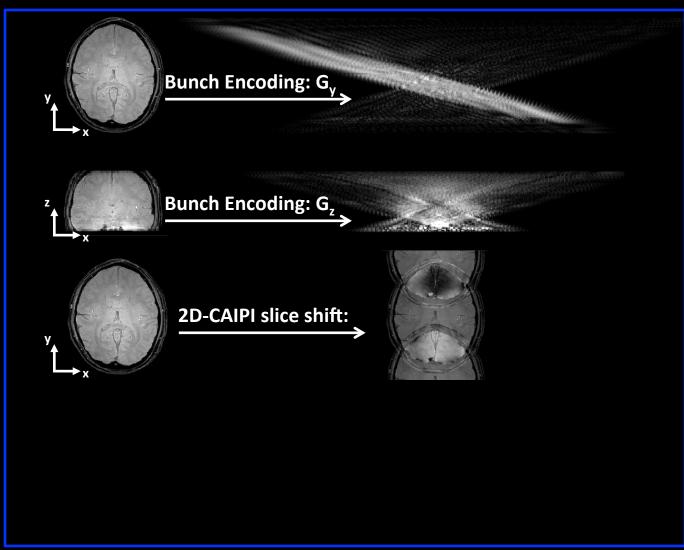


- Wave-CAIPI: 2D CAIPI + BPE in 2 direction
 - Spread <u>aliasing in 3D to take full advantage of 3D coil profiles</u>



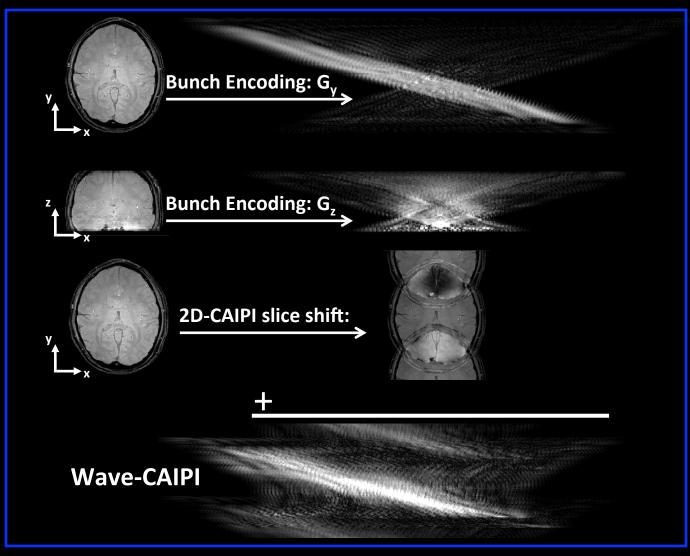
Effect of Wave Gradients

Combination of G_y and G_z gradients with interslice shifts yield voxel spreading across three dimensions



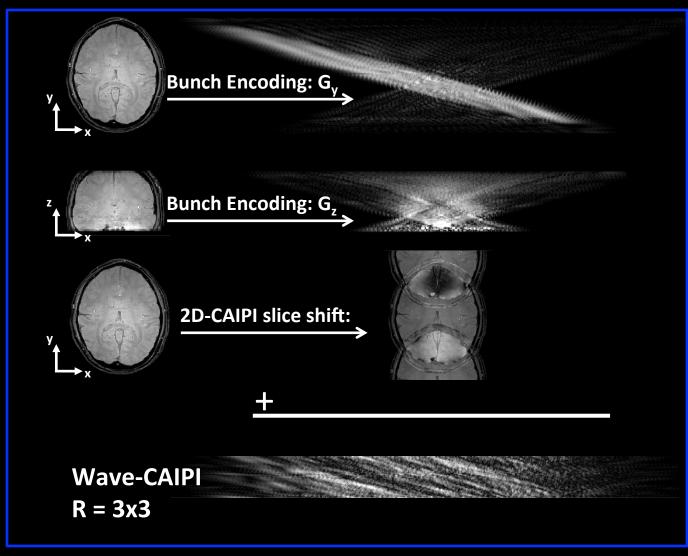
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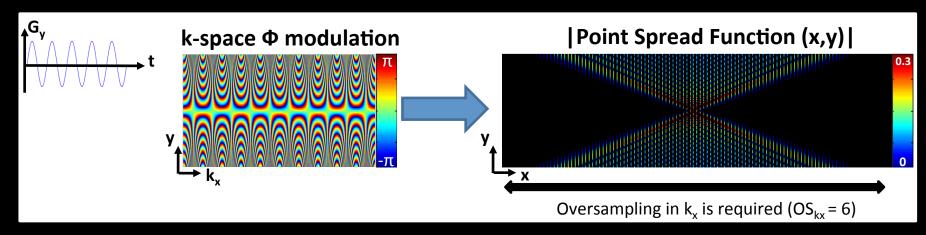


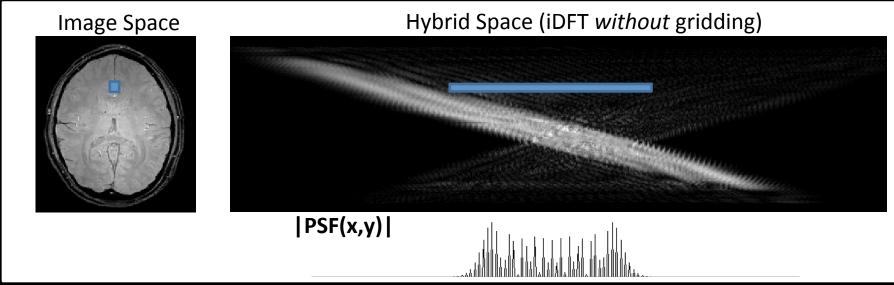
Effect of Wave Gradients

Combination of G_y and G_z gradients with interslice shifts yield voxel spreading across three dimensions



- Wave-CAIPI = $BPE G_y$ + BPE G_z + CAIPI 2D
- View BPE G_v as extra modulation rather than modifying k-space traj.





From signal equation:

$$wave(x,y,z) = \sum_{k_x} \mathrm{e}^{i2\pi x k_x/N} \cdot \mathrm{e}^{-i2\pi W_y(k_x)y} \cdot \sum_x \mathrm{e}^{-i2\pi x k_x/N} \cdot img(x,y,z)$$

$$wave(x,y,z) \qquad \text{Wave image}$$

$$img(x,y,z) \qquad \text{Underlying magnetization}$$

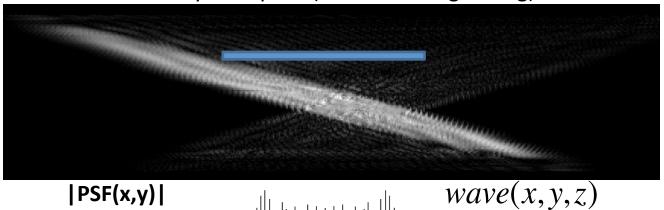
$$W_y(k_x(t)) = \frac{\gamma}{2\pi} \int_{0}^{t} G_y(\tau) d\tau \qquad \text{k-space trajectory}$$

Image Space



img(x, y, z)

Hybrid Space (iDFT without gridding)

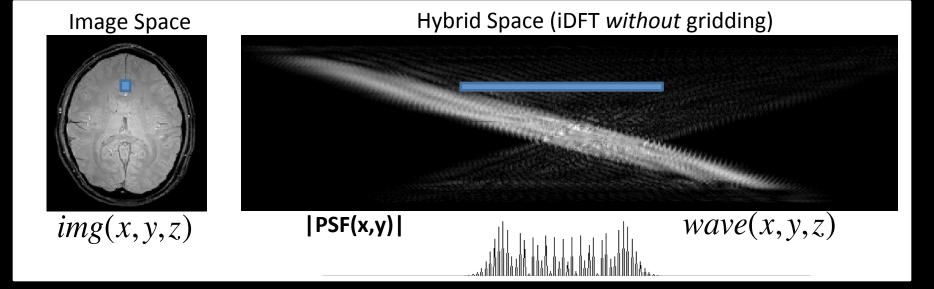


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Inverse Discrete
Fourier Transform

Discrete Fourier

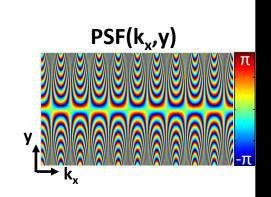
Transform

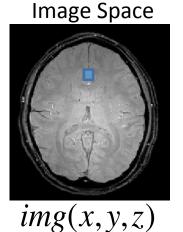


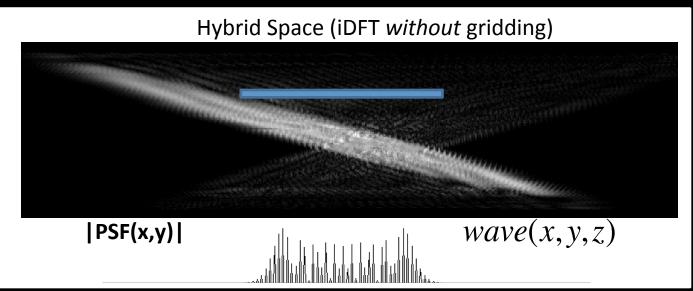
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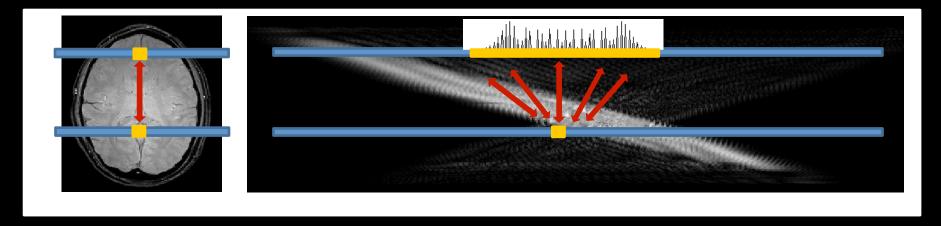
$$wave(x, y, z) = F^{-1} \cdot e^{-i2\pi W_y(k_x)y} \cdot F \cdot img(x, y, z)$$
Point Spread Function (PSF)

No need for gridding, simple DFT

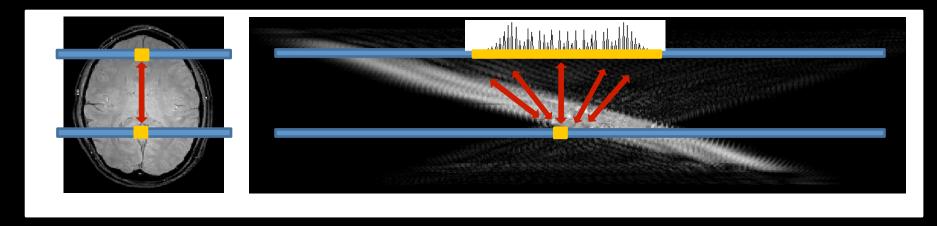








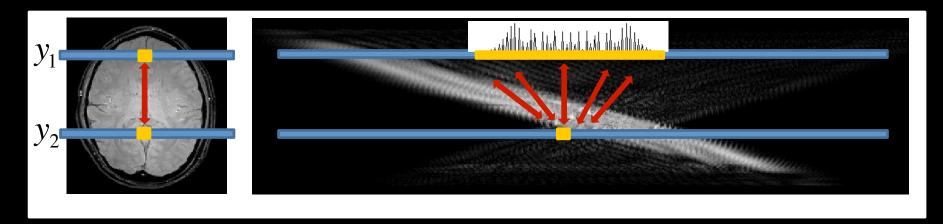
- $R_{inplane} = 2$
- => pair-wise aliasing of two rows of voxels
- => <u>small</u> Encoding matrix for each pair
- => separable and easy to solve
- => intuition on why Wave improves reconstruction



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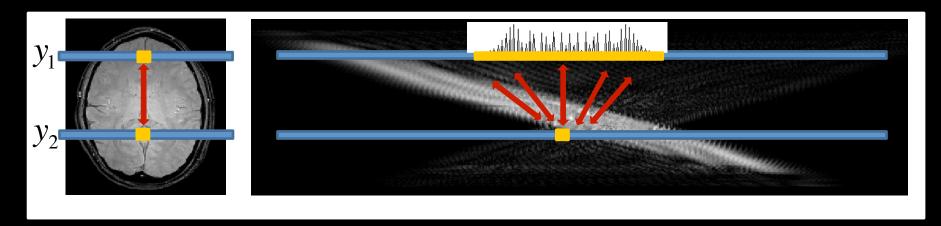
$$Psf(y)$$



- R_{inplane} = 2 => pair-wise aliasing of two rows of voxels
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$$wave(y) = F^{-1} \cdot Psf(y) \cdot F \cdot row(y)$$

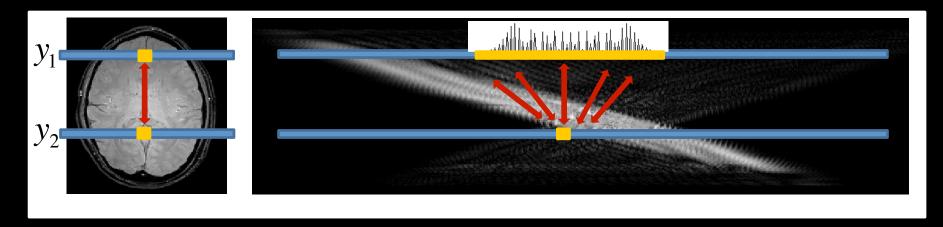
$$\begin{bmatrix} F^{-1} \cdot \operatorname{Psf}(y_1) \cdot F \\ F^{-1} \cdot \operatorname{Psf}(y_2) \cdot F \end{bmatrix} \cdot \begin{bmatrix} row(y_1) \\ row(y_2) \end{bmatrix} = [wave]$$



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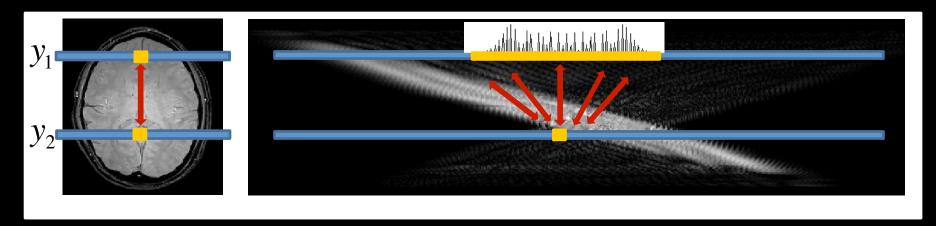
$$\begin{bmatrix} F^{-1} \cdot \operatorname{Psf}(y_1) \cdot F \cdot C(y_1) \\ F^{-1} \cdot \operatorname{Psf}(y_2) \cdot F \cdot C(y_2) \end{bmatrix} \cdot \begin{bmatrix} row(y_1) \\ row(y_2) \end{bmatrix} = [wave]$$



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$$\begin{bmatrix} F^{-1} \cdot Psf(y_1) \cdot F \cdot C_1(y_1) \\ \dots \\ F^{-1} \cdot Psf(y_2) \cdot F \cdot C_{32}(y_2) \end{bmatrix} \cdot \begin{bmatrix} row(y_1) \\ row(y_2) \end{bmatrix} = \begin{bmatrix} wave_1 \\ \dots \\ wave_{32} \end{bmatrix}$$
Encoding matrix



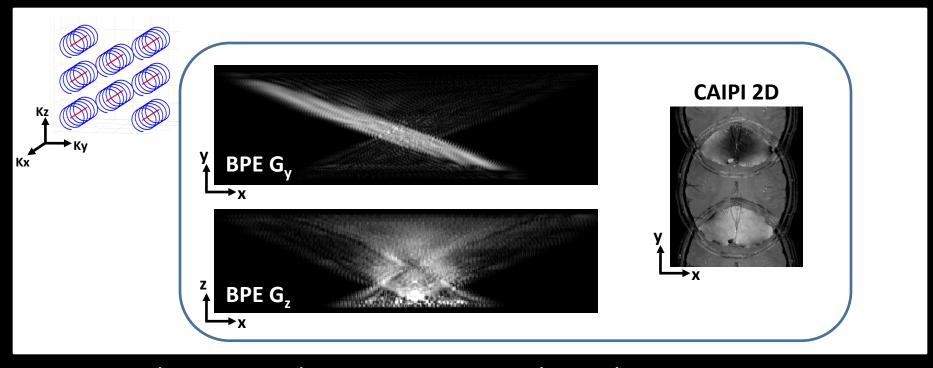
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Solve for each set of collapsed rows iteratively using LSQR

Wave-CAIPI reconstruction

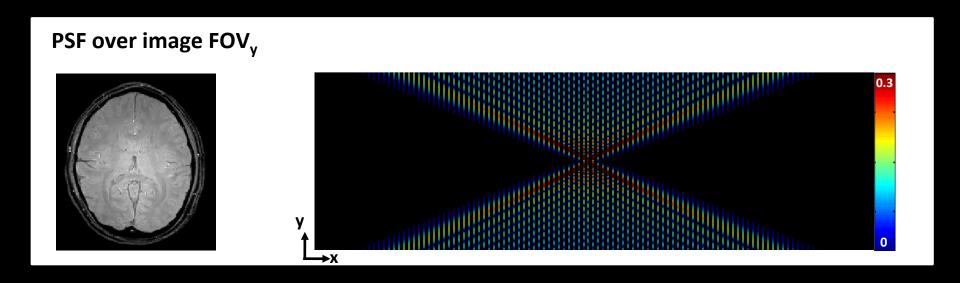


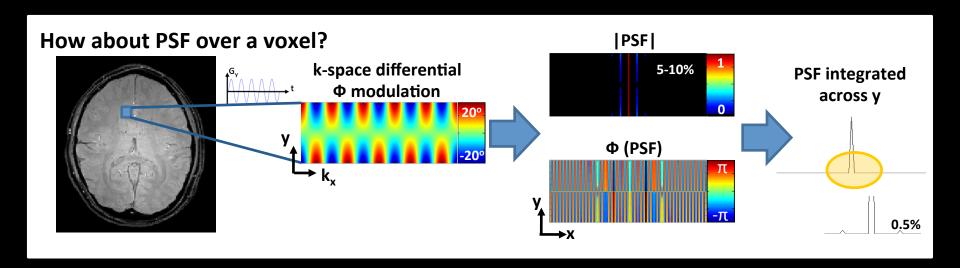
- \Rightarrow Wave gradients G_v and G_z create position dependent PSF
- ⇒ CAIPI 2D shift aliasing pattern
- ⇒ These are accounted for when generating the PSF-based Encoding matrices

$$\Rightarrow$$
 Ex: R = 3x3

- ⇒ each Encoding matrix corresponds to 9 rows of the image
- ⇒ grouping of rows is determined by CAIPI 2D
- \Rightarrow amount of spreading in each row determined by G_y and G_z

Artifact Quantification





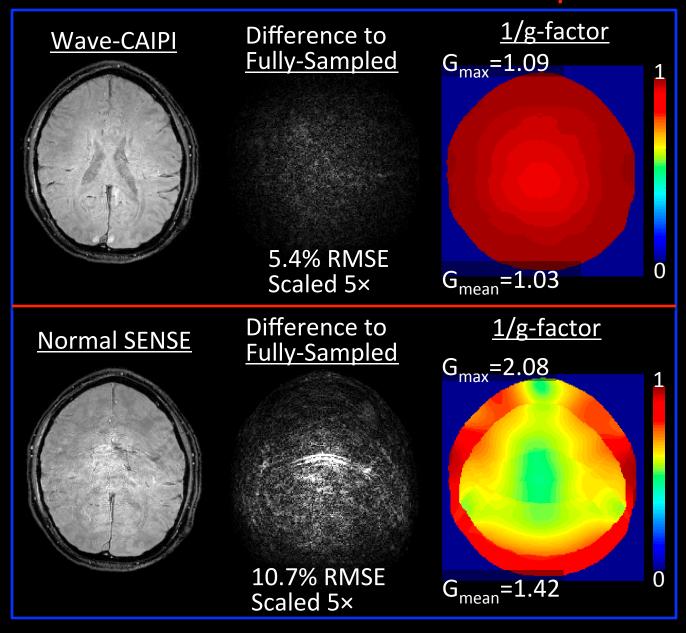
In Vivo Acquisition Comparison

- Compare Wave-CAIPI and conventional SENSE
- Acquire fully-sampled data, then accelerate by R = 3x3
- Compute root-mean-square error (RMSE) and 1/g-factor maps (retained SNR)

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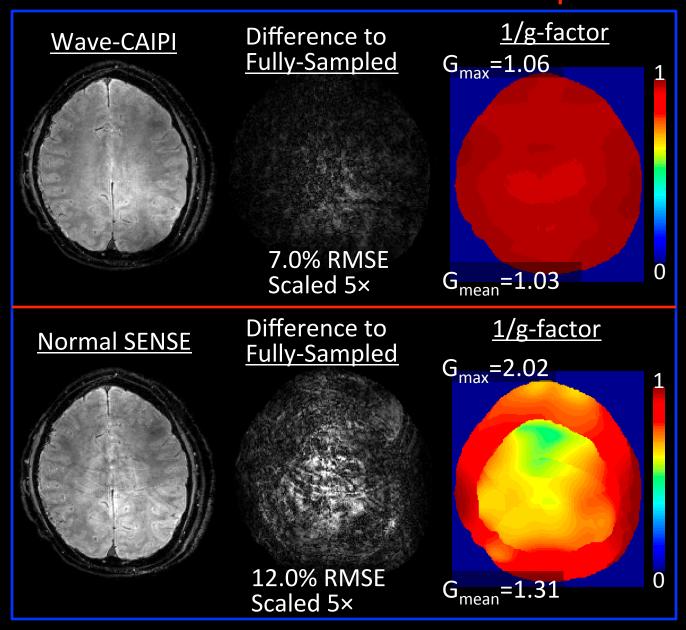
- Compare Wave-CAIPI and conventional SENSE
- Acquire fully-sampled data, then accelerate by R = 3x3
- Compute root-mean-square error (RMSE) and 1/g-factor maps (retained SNR)
- In vivo acquisitions:
 - At 3T and 7T
 - 1x1x2 mm resolution
 - 224x224x120 FOV

3 Tesla, R=3x3, 1x1x2 mm³, T_{acq}=38s



TR/TE = 26/13.3 ms

7 Tesla, R=3x3, 1x1x2 mm³, T_{acq}=40s



TR/TE = 27/10.9 ms

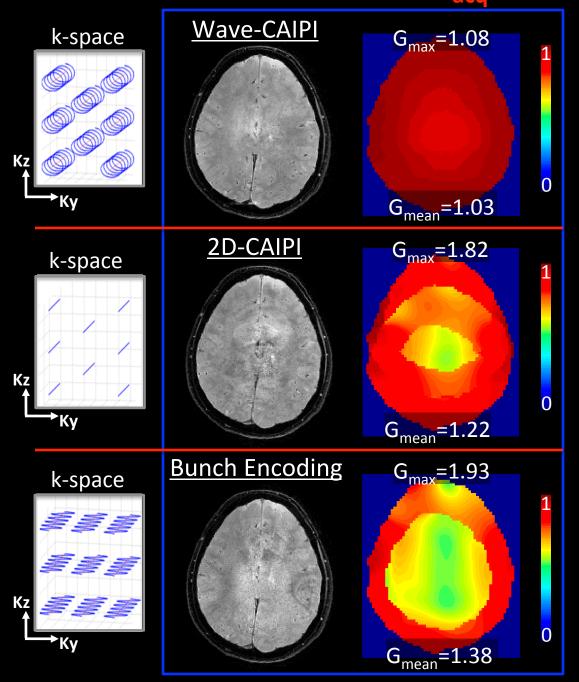
Accelerated Acquisition Comparison

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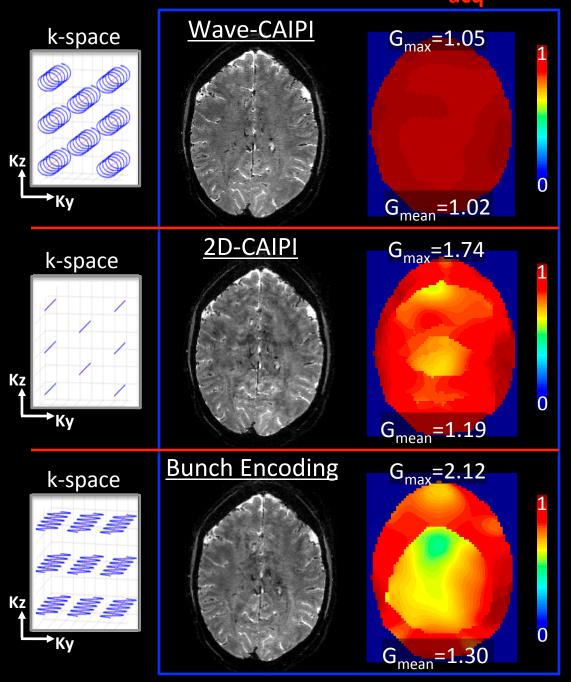
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- Acquire R = 3x3 accelerated data
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- In vivo acquisitions:
 - At 3T and 7T
 - 1x1x1 mm isotropic resolution
 - Acquisition time: 2.3 min
 - 240x240x120 FOV

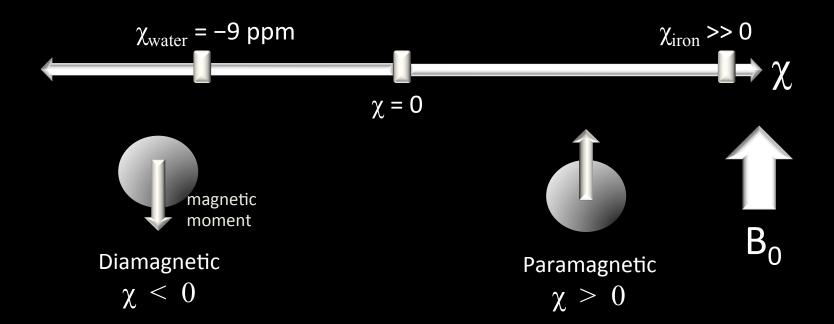
3 Tesla, R=3x3, 1x1x1 mm³, T_{acq}=2.3 min



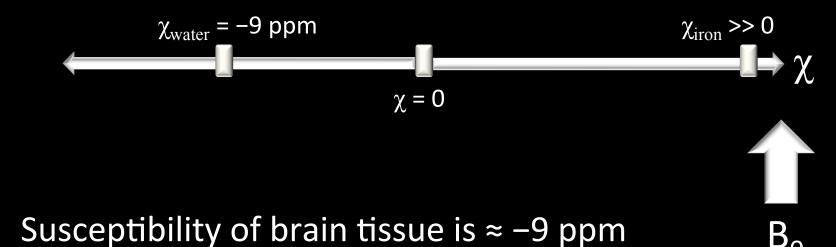
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 Susceptibility χ : degree of magnetization of a material when placed in a magnetic field

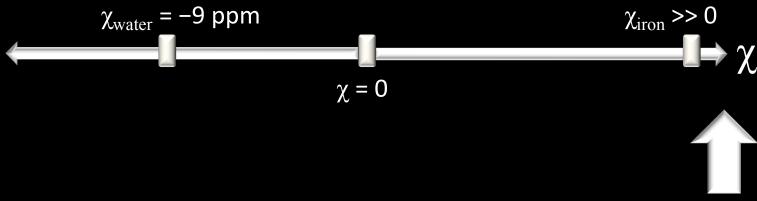


 Susceptibility χ : degree of magnetization of a material when placed in a magnetic field



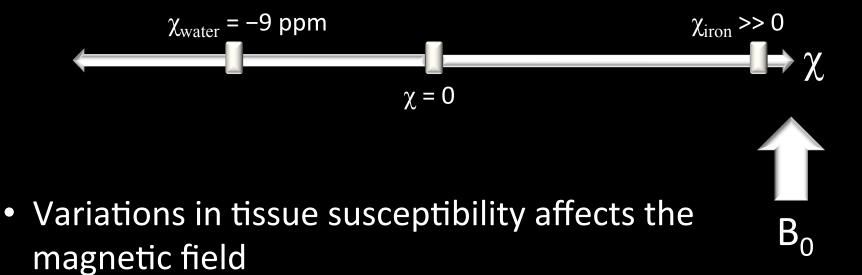
• Tissues with increased iron deposition are relatively paramagnetic $\rightarrow \chi$ is more positive

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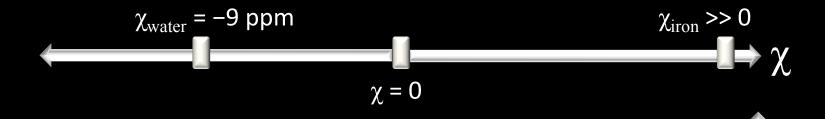
- Susceptibility of brain tissue is ≈ -9 ppm
- Tissues with increased iron deposition are relatively paramagnetic $\rightarrow \chi$ is more positive
- Excessive iron concentration occurs in a variety of degenerative diseases,
 - e.g. Alzheimer's, multiple sclerosis, Parkinson's

 Susceptibility χ : degree of magnetization of a material when placed in a magnetic field



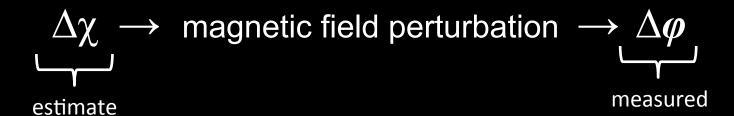
 $\Delta\chi$ \longrightarrow magnetic field perturbation

• Susceptibility χ : degree of magnetization of a material when placed in a magnetic field



 B_0

- Variations in tissue susceptibility affects the magnetic field
- Field perturbation causes a change in MR signal phase



Quantitative Susceptibility Mapping (QSM)

- Quantitative Susceptibility Mapping (QSM) aims to quantify tissue magnetic susceptibility with applications such as,
 - Tissue contrast enhancement¹
 - Estimation of venous blood oxygenation²
 - Quantification of tissue iron concentration³

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$$\delta = F^{-1}DF\chi$$

F: Discrete Fourier Transform

D: susceptibility kernel

 $\delta = \varphi/(\gamma \cdot TE \cdot B_0)$: normalized field map

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measured estimate

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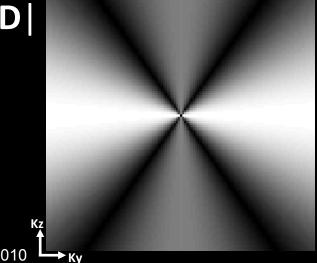
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 The inversion is made difficult by zeros in susceptibility kernel **D**

$$D = \frac{1}{3} - \frac{k_z^2}{k_x^2 + k_y^2 + k_z^2}$$

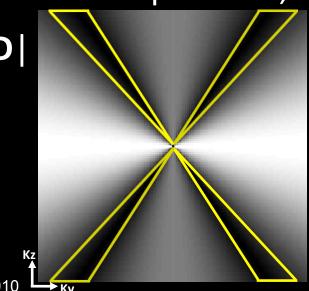


Quantitative Susceptibility Mapping (QSM)

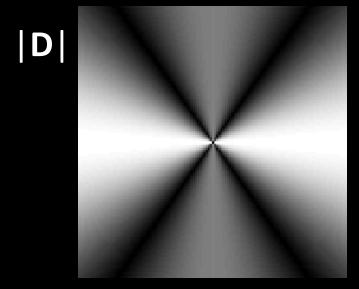
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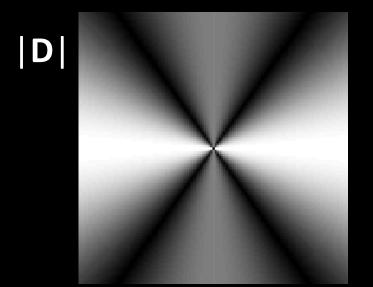
 Undersampling is due to physics Not in our control



Regularized Inversion for QSM

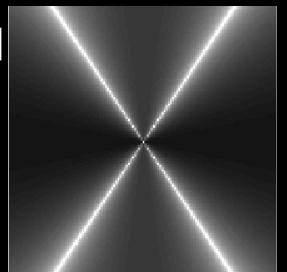


Regularized Inversion for QSM

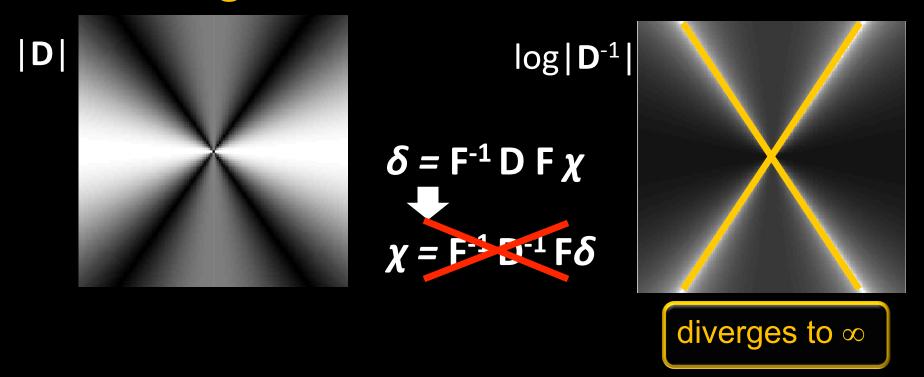


$$\delta = F^{-1} D F \chi$$

$$\mathbf{\chi} = F^{-1} D^{-1} F \delta$$



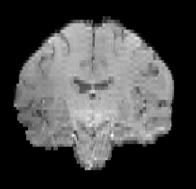
Regularized Inversion for QSM



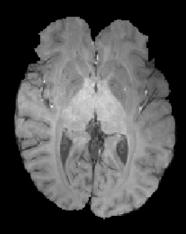
- Solving for χ by convolving with the inverse of **D** is not possible, as it diverges along the magic angle
- Use inverse problem formulation, apply regularization

Several processing steps are required to obtain the tissue phase

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 - i. Mask out the skull

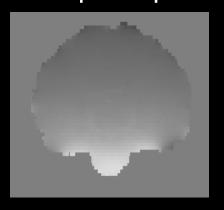


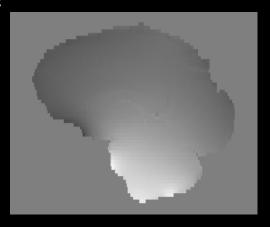


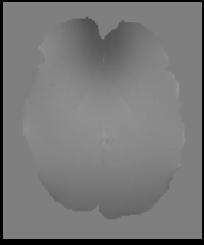


Using FSL Brain Extraction Tool¹

- Several processing steps are required to obtain the tissue phase
 - i. Mask out the skull
 - ii. Unwrap the phase







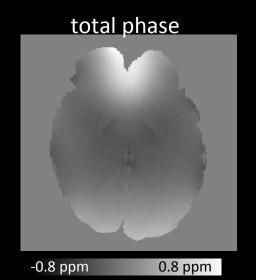
Using FSL PRELUDE¹

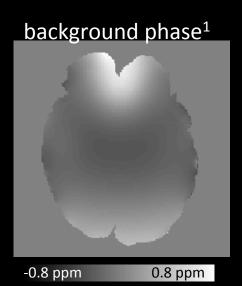
- Several processing steps are required to obtain the tissue phase
 - i. Mask out the skull
 - ii. Unwrap the phase

iii. Remove background phase

Phase accrued due to air-tissue interfaces needs to be removed.

This background component is ~10× larger than tissue phase.

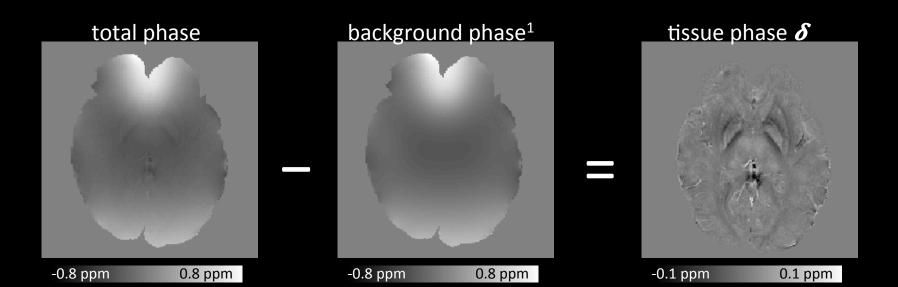




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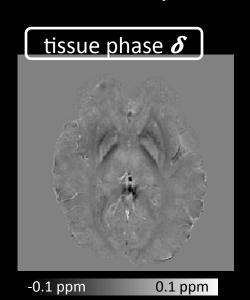


- Several processing steps are required to obtain the tissue phase
 - i. Mask out the skull
 - ii. Unwrap the phase
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Phase accrued due to air-tissue interfaces needs to be removed This background component is ~10× larger than tissue phase

• Now we can solve for χ from tissue phase δ

$$\delta = F^{-1}DF\chi$$



 We seek the susceptibility map that matches the observed tissue phase,

Find
$$\chi$$
 such that $\delta = F^{-1}DF\chi$

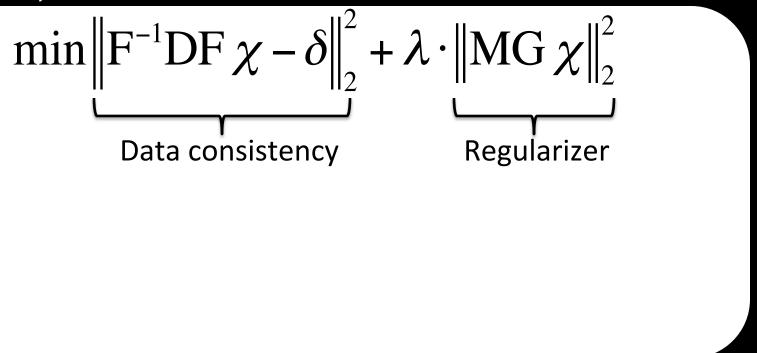
 Prior: Susceptibility is tied to the magnetic properties of the underlying tissue; hence it should vary smoothly within anatomical boundaries.

We seek the susceptibility map that matches the observed tissue phase,

Find
$$\chi$$
 such that $\delta = F^{-1}DF\chi$

- Prior: Susceptibility is tied to the magnetic properties of the underlying tissue; hence it should vary smoothly within anatomical boundaries.
- Employ regularization that encourages smoothness within tissues, but avoids smoothing across boundaries.

We solve for the susceptibility distribution with a convex program,



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$$\min \left\| \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \, \boldsymbol{\chi} - \boldsymbol{\delta} \right\|_{2}^{2} + \lambda \cdot \left\| \mathbf{M} \mathbf{G} \, \boldsymbol{\chi} \right\|_{2}^{2}$$

G: Spatial gradient operator in 3D

M: Binary mask derived from magnitude image, prevents smoothing across edges

 λ : Determines the amount of smoothness

We solve for the susceptibility distribution with a convex program,

$$\min \left\| \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \, \boldsymbol{\chi} - \boldsymbol{\delta} \right\|_{2}^{2} + \lambda \cdot \left\| \mathbf{M} \mathbf{G} \, \boldsymbol{\chi} \right\|_{2}^{2}$$

Optimizer given by the solution of:

$$(\mathbf{F}^{-1}\mathbf{D}^{2}\mathbf{F} + \lambda \cdot \mathbf{G}^{T}\mathbf{M}\mathbf{G})\chi = \mathbf{F}^{-1}\mathbf{D}^{T}\mathbf{F}\boldsymbol{\delta}$$

Large linear system, solve iteratively with Conjugate Gradient

We solve for the susceptibility distribution with a convex program,

$$\min \left\| \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \, \boldsymbol{\chi} - \boldsymbol{\delta} \right\|_{2}^{2} + \lambda \cdot \left\| \mathbf{M} \mathbf{G} \, \boldsymbol{\chi} \right\|_{2}^{2}$$

Optimizer given by the solution of:

$$(\mathbf{F}^{-1}\mathbf{D}^{2}\mathbf{F} + \lambda \cdot \mathbf{G}^{T}\mathbf{M}\mathbf{G})\chi = \mathbf{F}^{-1}\mathbf{D}^{T}\mathbf{F}\boldsymbol{\delta}$$

Without magnitude weighting (M=Identity), we proposed a closed-form solution:

$$\chi = (F^{-1}D^{2}F + \lambda \cdot G^{2})^{-1} \cdot F^{-1}D^{T}F\delta$$
Fast inversion
with two DFTs¹

 We solve for the susceptibility distribution with a convex program,

$$\min \left\| \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \, \boldsymbol{\chi} - \boldsymbol{\delta} \right\|_{2}^{2} + \lambda \cdot \left\| \mathbf{M} \mathbf{G} \, \boldsymbol{\chi} \right\|_{2}^{2}$$

Optimizer given by the solution of:

$$(\mathbf{F}^{-1}\mathbf{D}^{2}\mathbf{F} + \lambda \cdot \mathbf{G}^{T}\mathbf{M}\mathbf{G})\chi = \mathbf{F}^{-1}\mathbf{D}^{T}\mathbf{F}\boldsymbol{\delta}$$

Without magnitude weighting (M=Identity), we proposed a closed-form solution¹.

Using this inverse as preconditioner for Conjugate Gradient, we proposed a fast solution to the problem with magnitude weighting²

This improved computation speed 15-fold relative to existing solvers

Wave-CAIPI accelerated QSM

Wave-CAIPI enabled 3D GRE allows rapid QSM acquisition

- Compare in vivo phase and QSM from Wave-CAIPI, 2D-CAIPI and Bunch Phase Encoding:
 - At 3T and 7T
 - -R = 3x3 acceleration, scan time = 2.3 min
 - 1 mm isotropic resolution
 - TE = 20 ms, TR = 40 ms
 - 240x240x120 FOV

Wave-CAIPI accelerated QSM

Wave-CAIPI enabled 3D GRE allows rapid QSM acquisition

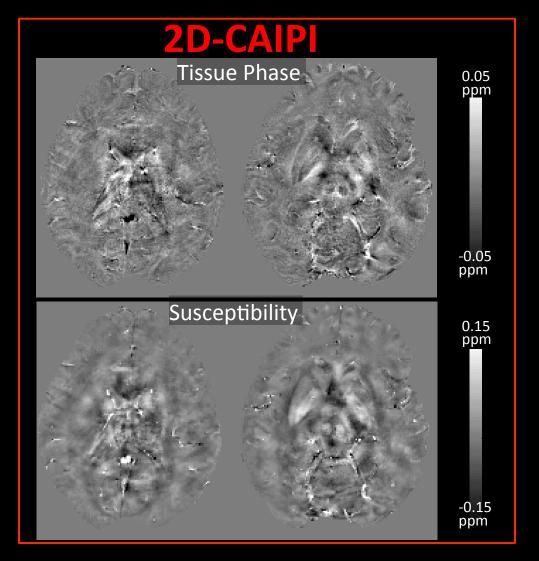
 Compare in vivo phase and QSM from Wave-CAIPI, 2D-CAIPI and Bunch Phase Encoding

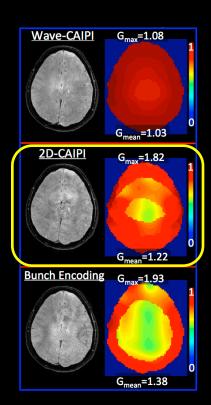
- Phase Processing:
 - Laplacian unwrapping¹ and
 - SHARP filtering for background removal²

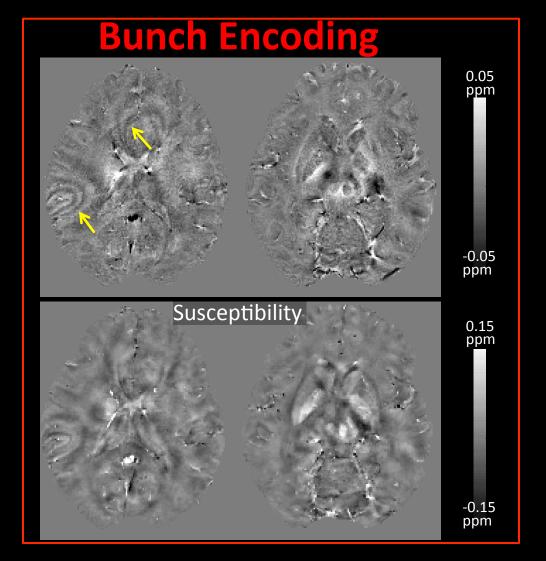
- 14 seconds

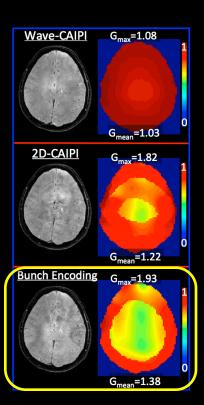
- Susceptibility Inversion:
 - Fast L2-regularized inversion³

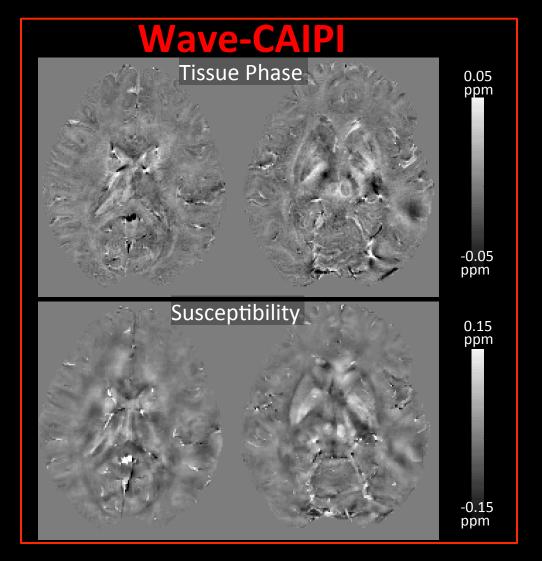
32 seconds

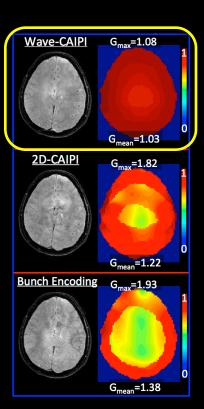


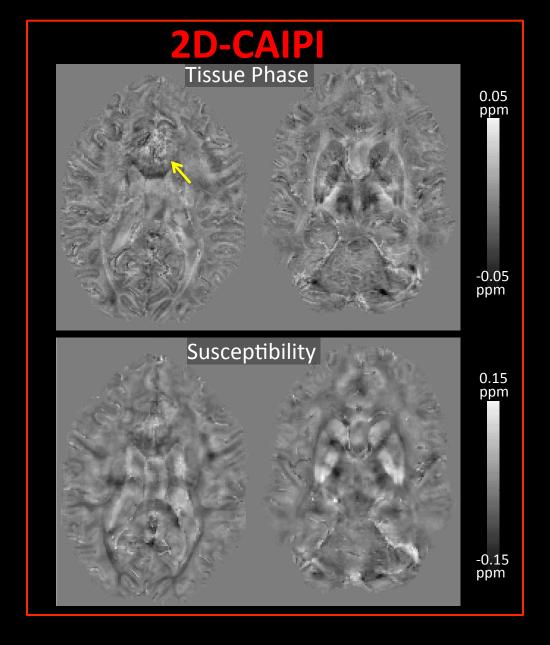


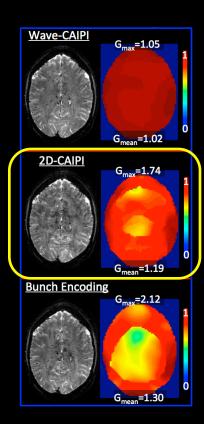


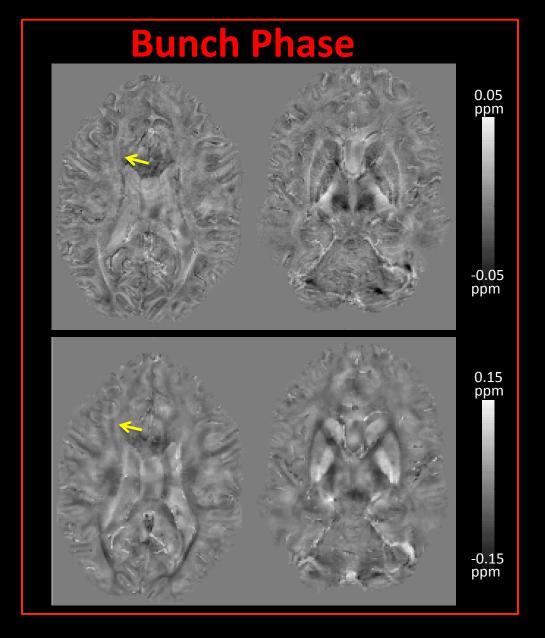


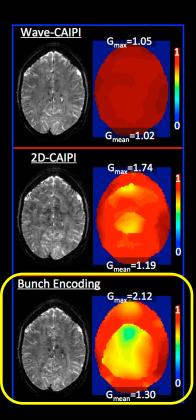


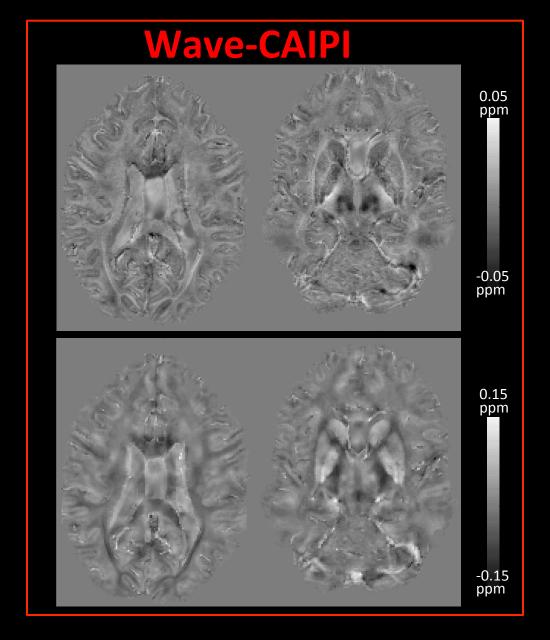


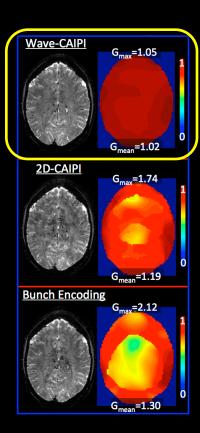












Summary

- Propose Wave-CAIPI acquisition/reconstruction scheme for highly accelerated 3D imaging
- Wave-CAIPI offers 2-fold improvement in g-factor and image artifact penalties compared to 2D-CAIPI and Bunch Phase Encoding

Summary

- Propose Wave-CAIPI acquisition/reconstruction scheme for highly accelerated 3D imaging
- Wave-CAIPI offers 2-fold improvement in g-factor and image artifact penalties compared to 2D-CAIPI and Bunch Phase Encoding
- Deployed in GRE imaging, Wave-CAIPI allows 9-fold acceleration with ~perfect SNR retention at 3T and 7T
- Combined with fast phase and susceptibility processing methods, it enables QSM at 1 mm resolution in 2.3 min

Thank you for your attention